Instructor: Phanuel Mariano

| Name: | Name: | KEY | |
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Instructions:

- All answers must be written clearly.
- You may use a calculator, but you must show all your work in order to receive credit.
- Be sure to erase or cross out any work that you do not want graded.
- If you need extra space, you may use the back sides of the exam pages (if you do, please write me a note so that I know where to look).
- You must include all work to receive full credit.

| Question: | 1 | 2 | 3 | 4 | 5 | 6 | Total |
|-----------|---|---|---|---|---|---|-------|
| Points: | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Score: | | | | | | | |

- 1. A certain state has license plates showing three numbers (0 through 9) and three letters (A through Z). How many different license plates are possible:
 - (a) If the numbers must come before the letters?

(b) If there is no restriction on where the letters and numbers appear?

- 2. Consider a standard deck of 52 cards.
 - (a) A gin hand consists of 10 cards from a standard deck of 52 cards. Find the probability that a gin hand has all 10 cards of the same suit.
 - (b) Find the probability that a gin hand has a three pair. (e.g. aabbccdefg)

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- 3. An urn contains 6 red, 4 blue, 8 green and 2 yellow balls. If a set of 4 balls is randomly selected (no replacement), what is the probability that each of the balls will be
 - (a) The same color?
 - (b) Of different colors?

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Red Blve Green $\frac{\binom{6}{4} + \binom{4}{4} + \binom{9}{4}}{\binom{20}{4}}$

$$\frac{\binom{6}{1}\binom{4}{1}\binom{9}{1}\binom{2}{1}}{\binom{20}{4}}$$

= .0793

= .6178

- 4. Independent flips of a coin that lands on heads with probability p are made. What is the probability that
 - (a) the first 10 outcomes are tails?

We have
$$P(H)=p$$
 and $P(T)=1-p$. Independent flips
imply that
$$P(T,T_1,...,T_{10})=P(T_1)P(T_2)\cdots P(T_{10})$$

$$=(1-p)^{10}$$

(b) the first 3 outcomes are heads?

(c) there are at least 1 heads in the first 10 outcomes?

E = at least t heads in 10 outromos
E'= ho heads in first 10 trials
= all 10 outrones are heads

$$P(E) = 1 - P(E') = 1 - (1-p)^{10}$$

- 5. A local college student goes to a bar 7 nights a week: 3 of the nights at bar A, 2 of the nights at bar B, and 2 of the nights at bar C. He'll get a girl's number 99 percent of the time at bar A, 96 percent of the time at bar B, and only 85 percent of the time at bar C.
 - (a) On a random night of the week, what is the probability that he gets a girl's number?

(b) Given that he doesn't get a girl's number, what is the probability that it was at bar C?

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6. Show that if $\mathbb{P}(A) > 0$, then $\mathbb{P}\left(A\cap B\mid A\right)\geq \mathbb{P}\left(A\cap B\mid A\cup B\right).$ X= P(ANBIA) Proof: Egl Y= IP CAMBIAUB) · Let's compute them separately Y= P(ANB LAUB) X= P(A NB LA) IP (ANB) Now since ACAUB, then by Proposition 1 IP(A) & P(AUB), which means P(A) Z Herefore X= P(APB) Z

which is what we manted to